**Peter Müller and Thibault Dardinier** 

# VIPER: AN INFRASTRUCTURE FOR AUTOMATED VERIFICATION IN SEPARATION LOGIC









- viper.ethz.ch
- Try online: http://viper.ethz.ch/tutorial
- Install as VS Code extension
- Tutorial: https://sites.google.com/view/viper tutorialpopl2025/home





### Outline

- Separation logic proofs in Viper
  - Hoare-style verification
  - Permission-based reasoning
  - Abstraction
  - Advanced separation logic
- Viper as target language
- Conclusion

## Basics of the Viper language

```
method indexOf(s: Seq[Int], e: Int) returns (res: Int)
  requires 0 < |s|</pre>
  ensures res < 0 ==> !(e in s)
  ensures 0 <= res ==> res < |s| && s[res] == e
  if(s[0] == e) { res := 0 }
  else {
    if(|s| == 1) { res := -1 }
    else {
      res := indexOf(s[1..], e)
      if(res != -1) { res := res + 1 }
```

- Viper is an imperative, statically-typed, sequential language
- Programs include a sequence of method declarations
- Methods have specifications
- Method bodies contain statements
  - Structured and unstructured control flow

## Type system

Viper has built-in primitive types with the usual operations

```
Bool, Int, ...
and built-in generic datatypes
Seq[T], Set[T], Multiset[T], Map[S,T]
```

Programs may declare generic ADTs and uninterpreted sorts (as part of custom theories)

```
adt List[T] {
    Nil()
    Cons(value: T, tail: List[T])
}
```

```
domain List[T] {
  function length(l: List[T]): Int
  axiom nonneg {
    forall l: List[T] :: 0 <= length(l)
  }
}</pre>
```

### Method specifications

method indexOf(s: Seq[Int], e: Int) returns (res: Int)
 requires 0 < |s|
 ensures res < 0 ==> !(e in s)
 ensures 0 <= res ==> res < |s| && s[res] == e
 decreases s</pre>

- Method specifications may include
  - Preconditions
  - Postconditions
  - A termination measure

- Viper verifies modularly that for all method executions
  - If the preconditions hold in the initial state then the execution will not abort and if the method terminates, the postconditions will hold in the final state
  - That the execution terminates, if a decreases clause is given

#### Loop annotations

```
method indexOf(s: Seq[Int], e: Int) returns (res: Int)
  ensures res < 0 ==> !(e in s)
  ensures 0 <= res ==> res < |s| && s[res] == e
  decreases s
  var i: Int := 0
  while(i < |s| && s[i] != e)</pre>
    invariant 0 <= i <= |s|</pre>
    invariant forall j: Int :: 0 <= j < i ==> s[j] != e
    decreases |s| - i
  { i := i + 1 }
  res := (i == |s| ? -1 : i)
}
```

- Verification of loops requires invariants
- Termination is verified if a decreases-clause is provided

### Outline

- Separation logic proofs in Viper
  - Hoare-style verification
  - Permission-based reasoning
  - Abstraction
  - Advanced separation logic
- Viper as target language
- Conclusion

### Heap model: an object-based language

```
field val: Int
method foo() returns (res: Int)
{
    var cell: Ref
    cell := new(val)
    cell.val := 5
    res := cell.val
}
```

- A heap maps object-field pairs to values
- No classes: each object has all fields declared in the entire program
  - Type rules of a source language can be encoded
  - Memory consumption is not a concern since programs are not executed
- Objects are accessed via references
  - Field read and update operations
  - No information hiding
- No explicit de-allocation
  - Conceptually, objects could remain allocated

### Access permissions

- Associate each heap location with a permission
- Permissions are held by method executions or loop iterations
- Read or write access to a memory location requires permission
- Permissions are created when the heap location is allocated
- Permissions can be transferred, but not duplicated or forged





### Permission assertions

#### **Separation logic**

 Separation logic denotes permissions by points-to predicates



 Disjointness of permissions is expressed by separating conjunction

 $p.f \mapsto _* q.f \mapsto _ \Rightarrow p \neq q$ 

#### Viper

- Viper's logic uses access predicates
  - Access predicates are not permitted under negations, disjunctions, and on the left of implications



 Viper's && acts like separating conjunction

acc(p.f) && acc(q.f)  $\Rightarrow$  p  $\neq$  q

# Verifying memory safety

- Memory safety is the absence of errors related to memory accesses, such as, null-pointer dereferencing, access to un-allocated memory, dangling pointers, outof-bounds accesses, double free, etc.
- Using permissions, Viper verifies memory safety by default



### Implicit dynamic frames

- Viper uses a variation of separation logic called implicit dynamic frames, which specify permissions and value constraints separately
- Assertions may contain both permissions and value constraints



 Most assertions that occur in a program must be self-framing, that is, include all permissions to evaluate the heap accesses in the assertion



### Implicit dynamic frames: example

```
method swap(a: Ref, b: Ref)
                                                     method swap(a: Ref, b: Ref)
  requires a.f \mapsto v * b.f \mapsto w
                                                       requires acc(a.f) && acc(b.f)
  ensures a.f \mapsto w * b.f \mapsto v
                                                       ensures acc(a.f) && acc(b.f)
                                                       ensures a.f == old(b.f) && b.f == old(a.f)
{
  var tmp: Int
  tmp := a.f
                                                       var tmp: Int
 a.f := b.f
                                                       tmp := a.f
                                                       a.f := b.f
  b.f := tmp
                                                       b.f := tmp
}
                                                     }
```

- old-expressions are evaluated in the pre-state of a method
- Labeled old-expressions allow one to relate arbitrary states within a method

#### Exercise

#### Implement a method

```
method gauss(n: Int, res: Ref)
```

that sums up the first n natural numbers and stores the result in the val-field of reference res.

Tasks:

- Verify memory safety.
- Specify and verify functional correctness.
- Verify termination.

Hints:

- See template Exercise1.vpr.
- Use a while loop.
- Store intermediate results directly in res.val, not in a local.



### Outline

- Separation logic proofs in Viper
  - Hoare-style verification
  - Permission-based reasoning
  - Abstraction
  - Advanced separation logic
- Viper as target language
- Conclusion

#### **Predicates**

 User-defined predicates consist of a predicate name, a list of parameters, and a self-framing assertion

```
predicate node(this: Ref) {
   acc(this.elem) && acc(this.next)
}
```

Recursive predicates may denote a statically-unbounded number of permissions

```
predicate list(this: Ref) {
   acc(this.elem) && acc(this.next) &&
   (this.next != null ==> list(this.next))
}
```

### Static verification with recursive predicates

A program verifier in general cannot know statically how far to unfold recursive definitions

```
predicate list(this: Ref) {
   acc(this.next) &&
   (this.next != null ==> list(this.next))
}
```

```
method client(x: Ref, y: Ref)
    requires list(x)
{
    y.next := null // do we have permission?
}
```

### **Iso-recursive predicates**

 An iso-recursive semantics distinguishes between a predicate instance and its body

```
predicate list(this: Ref) {
   acc(this.elem) && acc(this.next) &&
   (this.next != null ==> list(this.next))
}
```

```
method client(x: Ref)
   requires list(x)
{
   x.next := null // no permission
}
```

 Intuition: permissions are held by method executions, loop iterations, either directly or inside predicate instances

# Folding and unfolding predicates

- Exchanging a predicate instance for its body, and vice versa, is done via fold and unfold statements in the program
- An unfold statement exchanges a predicate instance for its body

```
method client(x: Ref)
   requires list(x)
{
    unfold list(x)
    x.next := null
}
```

 A fold statement exchanges a predicate body for a predicate instance

```
method client(x: Ref)
  requires list(x)
  ensures list(x)
{
   unfold list(x)
   x.next := null
   fold list(x)
}
```

 unfolding-expressions allow one to temporarily unfold a predicate during the evaluation of an expression

### Data abstraction

 To write implementation-independent specifications, we map the concrete data structure to mathematical concepts and specify the behavior in terms of those



## Data abstraction via abstraction functions

- Viper provides heap-dependent functions
  - side-effect free
  - terminating
  - deterministic
- Function bodies and function calls are expressions

```
function cont(this: Ref): Seq[Int]
  requires list(this)
{
   unfolding list(this) in
   (this.next == null ?
     Seq() :
     Seq(this.elem) ++ cont(this.next)
   )
}
```

- Functions may be recursive
- Functions must have a precondition that frames the function body, that is, provides all permissions to evaluate the body

## Idiomatic abstraction in Viper

```
predicate list(this: Ref, cont: Seq[Int]) {
  \exists e, n :: this.elem \mapsto e * this.next \mapsto n *
  (n == null ==> 0 == |cont|) *
  (n != null ==> ∃c ::
                   cont == Seq(e) ++ c *
                   list(n, c))
}
```

```
predicate list(this: Ref) {
  acc(this.elem) && acc(this.next) &&
  (this.next != null ==> list(this.next))
function cont(this: Ref): Seq[Int]
  requires list(this)
  unfolding list(this) in
  (this.next == null ?
    Seq() :
    Seq(this.elem) ++ cont(this.next)
```

- Implicit dynamic frames specify permissions and value constraints separately and separate inputs (this) from outputs (cont)
  - Facilitates incremental specification and verification
  - Enables using deterministic, side-effect free code functions in specifications (e.g., equals)

#### Exercise

Separation logic often uses predicates for list segments, for instance, to describe cyclic lists.

Tasks:

- Define a predicate 1seg for non-empty list segments.
- Define a function segcont that yields the sequence of integers stored in a list segment.
- Implement and verify a method

method single(e: Int) returns (res: Ref)

that creates a cyclic list with one element, e.

Hint:

See template Exercise2.vpr.

### Outline

- Separation logic proofs in Viper
  - Hoare-style verification
  - Permission-based reasoning
  - Abstraction
  - Advanced separation logic
- Viper as target language
- Conclusion

### **Fractional permissions**

- To distinguish read and write access, permissions can be split and re-combined
  - A permission amount  $\pi$  is a rational number in [0;1]
  - Viper syntax allows fractions n/d, as well as write for 1,
     none for 0, and wildcard for an arbitrary positive permission amount
  - acc(E.f) is a shorthand for acc(E.f, write), and
     P(E) for acc(P(E), write)
- Field read requires some non-zero permission, field write requires full (write) permission
- Separating conjunction sums up permissions of the conjuncts



## Sharing in data structures

Full permissions can describe tree-shaped data structures only

```
predicate person(this: Ref) {
    acc(this.savings) &&
    acc(this.savings.bal) }
```

Fractional permissions allow sharing

```
predicate person(this: Ref) {
   acc(this.savings) &&
   acc(this.savings.bal, 1/2) }
```

including unbounded (immutable) sharing

```
predicate person(this: Ref) {
  acc(this.savings &&
  acc(this.savings.bal, wildcard) }
```





## Predicates and fractional permissions

Predicates may contain fractions of permissions

```
predicate P(x: Ref)
{ acc(x.f, 1/2) }
```

It is also possible to own fractions of a predicate instance

acc(P(x), 1/2) && acc(P(x), 1/2) is

is equivalent to acc

acc(P(x), write)

 Unfold and fold multiply the fraction of the predicate with the fractions in the predicate body

```
method client(x: Ref)
  requires acc(P(x), 1/4)
  ensures acc(x.f, 1/8)
{
  unfold acc(P(x), 1/4)
}
```

## Limitations of recursive predicates

- Recursive predicates allow one to specify unbounded data structures
  - Traversals happen in the order in which the predicate needs to be unfolded
- Predicates are not ideal for many other use cases



Random-access data structures





Arbitrary cyclic data structures

### Quantified permissions

 To denote permission to an unbounded set of locations without prescribing a traversal order, we allow permissions and predicates to occur under universal quantifiers

forall x: ⊤ :: A

 Viper's forall quantifiers can be thought of as a possibly-infinite iterated separating conjunction

forall x: T ::  $A \equiv A[x_1/x] \&\& A[x_2/x] \&\& ...$ 

 Viper requires for each assertion acc(E.f) under a forall x:T that E is injective, that is:

 $x_1 \neq x_2 \Rightarrow E[x_1/x] \neq E[x_2/x]$ 

- The analogous rule applies to predicates (for parameter tuples)

## Explicit footprints

- As alternative to predicates, we can specify permission to an unbounded set of locations by
  - Maintaining an explicit set of references as ghost state (the explicit footprint)
  - Quantifying over the set elements in specifications



 We represent a graph as a set of nodes, each node stores a (possibly empty) set of successors

```
field next: Set[Ref]
predicate graph(nodes: Set[Ref]) {
   forall n: Ref :: n in nodes ==> acc(n.next) && (n.next subset nodes)
}
```

This idiom supports arbitrary traversals, random accesses, and arbitrary sharing

#### Partial data structures

```
field left: Ref
field right: Ref
predicate tree(x: Ref) {
  acc(x.left) && acc(x.right)
  && (x.left != null ==> tree(x.left))
  && (x.right != null ==> tree(x.right))
method getLeft(x:Ref) returns (y:Ref)
  requires tree(x)
  ensures tree(y) && ...
{
  y := x
  while (y.left != null)
    invariant tree(y) && ...
    unfold tree(y)
```

y := y.left

 To allow clients of getLeft to use the predicate tree(x) later, getLeft needs to return permissions to the rest of the tree



- Not ideal: define a dedicated predicate
  - Requires a way to identify the hole
  - Requires ghost code to plug the hole

## Separating implication: magic wands

A magic wand P -\* Q represents the difference between Q and P



This allows us to specify our getLeft method

```
method getLeft(x: Ref) returns (y: Ref)
  requires tree(x)
  ensures tree(y) && (tree(y) --* tree(x))
```

 Intuition: permissions are held by method executions, loop iterations, either directly or inside predicate instances or magic wands

## Reasoning with magic wands

- Applying a magic wand
  - Viper has a designated statement to apply modus ponens for magic wands



- Creating a magic wand
  - Viper needs to determine which permissions from the current state need to be moved into the wand such that the wand, together with **P**, yields **Q**



### Example revisited

```
method getLeft(x: Ref) returns (y: Ref)
    requires tree(x)
    ensures tree(y) && (tree(y) --* tree(x))
{
   v := x
   package tree(x) --* tree(x)
   while (unfolding tree(y) in y.left != null)
      invariant tree(y) && (tree(y) --* tree(x))
   ł
      unfold tree(y)
      var y left: Ref := y.left
      package tree(y_left) --* tree(x)
         fold tree(y)
         apply tree(y) --* tree(x)
      y := y_left
```

```
y := getLeft(x)
y.update() // requires tree(y)
apply tree(y) --* tree(x)
x.update() // requires tree(x)
```

## The Viper language

#### **Program code**

- Sequential, imperative language
- Standard control structures
- Basic type system
- Built-in heap
- Explicit permission manipulation

#### Assertion language

- Inductive predicates
- Abstraction functions
- Fractional permissions
- Iterated separating conjunction
- Magic wands

#### Verification

- Absence of run-time errors
- Memory safety
- User-provided assertions
- Termination

#### Mathematical theories

- Predefined datatypes
- User-defined datatypes
- Uninterpreted functions
- Axioms



### Outline

- Separation logic proofs in Viper
- Viper as target language
  - Encoding source languages
  - Encoding program logics
- Conclusion

### Example: Go verification in Gobra

```
requires acc(x) && acc(y)
ensures acc(x) && acc(y)
ensures *x == old(*y)
ensures *y == old(*x)
func swap(x *int, y *int) {
    tmp := *x
    *x = *y
    *y = tmp
}
```

- Go supports pointers to integers
- Parameters can be assigned to
- Locals get initialized by default

#### field val: Int

```
method swap(x: Ref, y: Ref)
 requires acc(x.val) && acc(y.val)
 ensures acc(x.val) && acc(y.val)
 ensures x.val == old(y.val)
 ensures y.val == old(x.val)
 var yLocal: Ref // declare locals
 var xLocal: Ref
 xLocal := x // copy parameters
 yLocal := y
 var tmp: Int // declare tmp
 tmp := 0
 tmp := xLocal.val // tmp = *x
 xLocal.val := yLocal.val // *x = *y
 yLocal.val := tmp // *y = tmp
```

### Arrays

- Viper does not have built-in arrays
- In contrast to sequences, arrays are mutable heap data structures
- We model arrays by a set of disjoint references that can be accessed via an index
- loc(a, i).val models a[i]
- More-dimensional arrays can be encoded analogously

field val: Int // for integer arrays

```
domain Array {
  function loc(a: Array, i: Int): Ref
  function len(a: Array): Int
  function first(r: Ref): Array
  function second(r: Ref): Int
  axiom injectivity {
```

```
forall a: Array, i: Int :: {loc(a, i)}
    first(loc(a, i)) == a &&
    second(loc(a, i)) == i
}
```

```
axiom length_nonneg {
  forall a: Array :: len(a) >= 0
```

### Accessing array locations

- Arrays are random-access data structures
- We can express permissions using quantified permissions

forall i: Int :: 0 <= i < len(a) ==> acc(loc(a, i).val)

- Similarly for sub-ranges of the array
- We define macros for convenient access



define update(a, i, e) {
 loc(a, i).val := e
}

- Bounds are checked implicitly via permissions

### Outline

- Separation logic proofs in Viper
- Viper as target language
  - Encoding source languages
  - Encoding program logics
- Conclusion

#### Permission transfer



method client(x: Ref, y: Ref) requires acc(x.f) && acc(y.f) requires x.f == 2 && y.f == 7 { X ? 7 Framing! set(x, 5)**assert** x.f == 5 && y.f == 7

### Permission transfer for method calls



- Calling a method transfers permissions from the caller to the callee (according to the method precondition)
- Returning from a method transfers permissions from the callee to the caller (according to the method postcondition)
- Residual permissions are framed around the call

#### Permission transfer for loops and concurrency





### Permission transfer: inhale and exhale operations

- inhale A means:
  - obtain all permissions required by assertion A
  - assume all logical constraints



- exhale A means:
  - assert all logical constraints
  - check and remove all permissions required by assertion A
  - havoc any locations to which all permission is lost



## Encoding of method bodies and calls

```
method foo() returns (...)
   requires A
   ensures B
{ S }
```

x := foo()

Encoding with heap

Encoding without heap and globals



inhale and exhale are permission-aware analogues of assume and assert

### Encoding structured parallelism

• The proof rule employs the familiar permission transfer

$$\begin{array}{c|c} \left\{ \begin{array}{c} \textbf{A}_{1} \end{array} \right\} & \left\{ \begin{array}{c} \textbf{B}_{1} \end{array} \right\} & \left\{ \begin{array}{c} \textbf{A}_{2} \end{array} \right\} & S_{2} \end{array} \left\{ \begin{array}{c} \textbf{B}_{2} \end{array} \right\} \\ \hline \left\{ \begin{array}{c} \textbf{A}_{1} \ast \textbf{A}_{2} \end{array} \right\} & S_{1} \parallel S_{2} \end{array} \left\{ \begin{array}{c} \textbf{B}_{1} \ast \textbf{B}_{2} \end{array} \right\} \\ \hline \left\{ \begin{array}{c} \textbf{A}_{1} \ast \textbf{A}_{2} \ast \textbf{C} \end{array} \right\} & S_{1} \parallel S_{2} \end{array} \left\{ \begin{array}{c} \textbf{B}_{1} \ast \textbf{B}_{2} \ast \textbf{C} \end{array} \right\} \end{array}$$

We can encode this proof rule via exhale and inhale operations

```
method S<sub>1</sub>(...) returns (res<sub>1</sub>: T)
    requires A<sub>1</sub>
    ensures B<sub>1</sub>
    { // encoding of S<sub>1</sub> }
```

Encode left and right branch as methods with specifications

```
exhale A<sub>1</sub>[...]
exhale A<sub>2</sub>[...]
havoc res<sub>1</sub>, res<sub>2</sub>
inhale B<sub>1</sub>[...]
inhale B<sub>2</sub>[...]
```

Encode parallel composition like two half method calls

### **Encoding locks**

{ **R** } x := new Lock() { isLock(x, **R**) }

{  $isLock(x, \mathbf{R})$  } acquire x {  $locked(x, \mathbf{R}) * \mathbf{R}$  }

{ locked(x,  $\mathbf{R}$ ) \*  $\mathbf{R}$  } release x { isLock(x,  $\mathbf{R}$ ) }

 $\forall x :: isLock(x, \mathbf{R}) \Leftrightarrow isLock(x, \mathbf{R}) * isLock(x, \mathbf{R})$ 

Encode custom resources as abstract predicates

predicate isLock(x: Ref, ...)

predicate locked(x: Ref, ...)

Encode duplicable resources as arbitrary positive fractions

acc(isLock(x, ...), wildcard)

## **Encoding lock invariants**

{ **R** } x := new Lock() { isLock(x, R) }

{ isLock(x,  $\mathbf{R}$ ) } acquire x { locked(x,  $\mathbf{R}$ ) \*  $\mathbf{R}$  }

{ locked(x, R) \* R } release x { isLock(x, R) }

 $\forall x :: isLock(x, \mathbf{R}) \Leftrightarrow isLock(x, \mathbf{R}) * isLock(x, \mathbf{R})$ 

 Specify invariant in a program annotation



- Declare macro or predicate for all invariants

define Inv(x, n) (
 (n == c ==> R) &&
 ...
)

### **Encoding lock operations**

{ **R** } x := new Lock() { isLock(x, **R**) }

{ isLock(x, R) } acquire x { locked(x, R) \* R }

{ locked(x, R) \* R } release x { isLock(x, R) }

 $\forall x :: isLock(x, \mathbf{R}) \Leftrightarrow isLock(x, \mathbf{R}) * isLock(x, \mathbf{R})$ 

exhale Inv(x,c)
inhale acc(isLock(x, c), wildcard)

exhale acc(isLock(x, c), wildcard)
inhale locked(x, c) && Inv(x,c)

exhale locked(x, c) && Inv(x,c)
inhale acc(isLock(x, c), wildcard)

#### Exercise

The following rules are adapted from Relaxed Separation Logic.

 $\{true\} \ l := alloc_{na}() \ \{Uninit(l)\}$ 

$$\{l \stackrel{\scriptscriptstyle 1}{\mapsto} \_ \lor \mathsf{Uninit}(l)\} \ [l]_{\mathsf{na}} := e \ \{l \stackrel{\scriptscriptstyle 1}{\mapsto} e\}$$

$$\{l \stackrel{k}{\mapsto} e\} x := [l]_{na} \{x = e * l \stackrel{k}{\mapsto} e\}$$
$$(l \stackrel{k}{\mapsto} e * l \stackrel{k'}{\mapsto} e') \Leftrightarrow (e = e' * l \stackrel{k+k'}{\mapsto} e)$$

Encode them in Viper and verify the client code on the right.

- Assume that I is an integer location.
- Recall that Viper does not support disjunction of impure assertions.

Hints:

- See template Exercise3.vpr.
- Track initialization in the state.

```
method sum(p, q)
   requires p \stackrel{\frac{1}{2}}{\mapsto} v * q \stackrel{\frac{1}{2}}{\mapsto} w
   ensures p \stackrel{\frac{1}{2}}{\mapsto} v * q \stackrel{\frac{1}{2}}{\mapsto} w
   ensures result == v + w
{
   a := [p]
   b := [q]
   return a + b
}
method client() {
   x := alloc()
   y := alloc()
   [x] := 2
   [y] := 3
   s := sum(x, y)
   assert s == 5
```

## Scope of existing Viper encodings

#### Language features

- Imperative code
- Object-oriented code
- Nominal and structural typing
- Closures
- Multithreading with shared state and message passing
- Weak-memory concurrency

#### **Properties**

- Memory safety
- Absence of overflows
- Termination
- Functional correctness
- Race freedom
- Linearizability
- Deadlock freedom
- Secure information flow
- Resource manipulation
- Worst-case execution time

### Outline

- Separation logic proofs in Viper
- Viper as target language
- Conclusion



### Main limitations

#### Inherited from SMT solver

- First-order logic
- Undecidable theories may lead to spurious errors
- Verification time for large methods

#### **Annotation overhead**

 Typically 2-5 lines of annotations per line of code

#### **Trust assumptions**

- Correctness of SMT solver
- Correctness of Viper
- Correctness of front-end encoding

#### Formal Foundations for Translational Separation Logic Verifiers



Talk on Wednesday at 5pm in Peek-A-Boo!

# Verifiers developed at ETH



P\*rust-\*i

- Verification infrastructure for permission-based reasoning
- Basis for our other verifiers
- viper.ethz.ch

- Modular verification of Go programs
- Used for large-scale verification projects, e.g., verifiedSCION
- gobra.ethz.ch

- Modular verification of Rust programs
- Leverages Rust type system to simplify verification
- prusti.ethz.ch



- Modular verification of Python programs
- Correctness and security properties
- Variant for Ethereum smart contracts in Vyper
- www.pm.inf.ethz.ch/research/ nagini.html